

PHILADELPHIA UNIVERSITY
DEPARTMENT OF BASIC SCIENCES

Module:	Modern Euclidean Geometry	Paper:	Final Exam
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Problems 1 to 6: Circle the best choice, 2 points each.

1. Three lines are concurrent; the meaning is
 - (a) they all intersect at one point
 - (b) they are all parallel
 - (c) they are all congruent to each other
 - (d) they are not parallel to each other

2. What is a definition of $AB < CD$?
 - (a) there is E such that $A*B*E$ and $BE \approx CD$
 - (b) there is E such that $C*D*E$ and $CE \approx AB$
 - (c) there is E such that $A*E*B$ and $AE \approx CD$
 - (d) there is E such that $C*E*D$ and $CE \approx AB$

3. What is a bisector of $\angle BAC$?
 - (a) a line that intersects both lines AB and AC
 - (b) a ray AD between AB and AC such that $\angle BAD \approx \angle DAC$
 - (c) half of the angle BAC
 - (d) any point D which is interior of $\angle BAC$

4. There exist 3 points which are not collinear. The negation of this statement is
 - (a) There are 3 points which are collinear.
 - (b) There are less than 3 points which are not collinear.
 - (c) Given 3 points, they are collinear.
 - (d) Given a line, there exist 3 points on the line.

5. Given a line l and a point P not on l. Which statement cannot be proved in Neutral Geometry?
 - (a) There exists a line through P perpendicular to l.
 - (b) There exists a unique line through P perpendicular to l.
 - (c) There exists at least one line through P parallel to l.
 - (d) There exists a unique line through P parallel to l.

6. AAA is a theorem in
 - (a) Neutral Geometry
 - (b) Hyperbolic Geometry only
 - (c) Euclidean Geometry only
 - (d) Euclidean and Hyperbolic Geometries

Problems 7 to 10 are related to the following model, 2 points each.

Points: A, B, C, D, E

Lines: {A, B}, {A, C}, {C, D}, {B, C, E}, {D, E}

7. In this model the Incidence Axiom 1 is (a) true (b) false.
8. In this model the Incidence Axiom 2 is (a) true (b) false.
9. In this model the Incidence Axiom 3 is (a) true (b) false.
10. This model satisfies the parallel postulate of
 - (a) Euclidean geometry
 - (b) Elliptic geometry
 - (c) Hyperbolic geometry
 - (d) none of them

Problems 11 to 13: Give the definitions, 2 points each.

11. the opposite of ray AB
12. A and B are on opposite sides of a line l
13. $\angle BAC < \angle EDF$

Problems 14 to 16: Write the propositions in detail, 2 points each.

14. Angle Addition
15. SAA Criterion
16. Alternate Interior Angle Theorem

Problems 17 to 19 are related to the following axioms, 2 points each.

Axiom 1: There exist 2 parallel lines

Axiom 2: There exist 3 points which are collinear

Axiom 3: Given 2 points, there exists a unique line incident with them

17. Give a model such that Axioms 1, 2, 3 are all true.

18. Give a model such that only Axiom 1 is true, the others false.

19. Give a model such that only Axiom 2 is true, the others false.

20. Fill in the blanks to complete the proof, 2 points each.

Given $\triangle ABC$ and $\triangle ABD$ where C and D are on opposite sides of line AB.
If $AC \approx AD$ and $BC \approx BD$ then $\triangle ABC \approx \triangle ABD$.

Proof.

1. $\angle ACD \approx \angle ADC$ ()
2. $\angle BCD \approx \angle BDC$ (same as 1)
3. $\angle ACB \approx \angle ADB$ ()
4. $\triangle ABC \approx \triangle ABD$ ()

21. Prove the following proposition, 6 points each.

Given $\angle BAC$ and a point D on the line BC.

Prove that if D is in the interior of $\angle BAC$ then B^*C^*D .