

PHILADELPHIA UNIVERSITY  
DEPARTMENT OF BASIC SCIENCES

Exam 1

Number Theory

19–03–2014

Solutions must be complete in order to receive full credit.

1. Evaluate  $\gcd(m, n)$  and find integers  $a, b$  such that  $\gcd(m, n) = am + bn$ , for the numbers  $m = 1254$  and  $n = 532$ .
2. Find all the integer solutions to the linear equation  $27x + 72y = 63$ .
3. Prove that  $12 \mid n^4 - n^2$  for any integer  $n$ .
4. Determine  $n$  is prime or composite, using trial division, with  $n = 667$ .
5. Count how many divisors of the number  $n = 11520$ .
6. Factor  $m$  and  $n$  using prime numbers and evaluate  $\gcd(m, n)$ , for the numbers  $m = 435600$  and  $n = 457600$ .

–Amin Witno

The list of primes below 200.

2	3	5	7	11	13	17	19	23	29
31	37	41	43	47	53	59	61	67	71
73	79	83	89	97	101	103	107	109	113
127	131	137	139	149	151	157	163	167	173
179	181	191	193	197	199				